

# Spatially separated excitons in 2D and 1D

David Abergel

March 10th, 2015



NORDITA



**European Research Council**

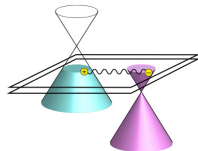
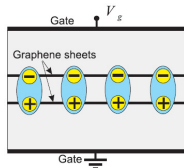
Established by the European Commission

- 1 Introduction
- 2 Spatially separated excitons in 2D – The role of disorder
- 3 Spatially separated excitons in 1D

# Introduction

Key ingredients:

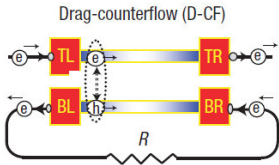
- Independent contacts to each layer
- High degree of nesting of Fermi surfaces
- Low SP tunneling rate between layers



Picture credit: Kharitonov *et al.*, Phys. Rev. B **78**

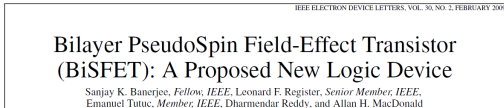
Phase coherence between the two layers

Transport of excitons can be measured:



Picture credit: Su *et al.*, Nat. Phys. **4**.

Apply current in lower layer, measure voltage drop in upper layer (drag measurement).





## A new mechanism for superconductivity: pairing between spatially separated electrons and holes

Yu. E. Lozovik and V. I. Yudson

*Spectroscopy Institute, USSR Academy of Sciences*  
(Submitted March 2, 1976)  
Zh. Eksp. Teor. Fiz. **71**, 738–753 (August 1976)

A new mechanism for superconductivity, based on the pairing of spatially separated electrons and holes that arises from their Coulomb attraction, is proposed. A gap in the single-particle excitation spectrum is found. The roles of interband transitions, the electron-phonon interaction, scattering by impurities, spin-orbit interaction, etc. are analyzed. The critical current is calculated. Possible experiments are discussed.

PACS numbers: 74.30. – e

The maximum value of the gap  $\Delta$ , equal in order of magnitude to the binding energy  $E_0 = m^* e^4 / \epsilon^2$  of an isolated pair, is attained when  $m_e \sim m_h \sim m^*$  and  $D \lesssim a^* \sim l$  (the strong-interaction regime, in which (8) has only the character of an estimate;  $a^* = \epsilon / m^* e^2$ ). If, e.g.,  $m^* = 0.03 m_0$  ( $m_0$  is the electron mass) and  $\epsilon = 3$ , then  $a^* \approx 50 \text{ \AA}$  and for  $D \sim l \sim 50 \text{ \AA}$  we have  $\Delta \sim 300 \text{ K}$ .

Prediction was formation of 'superconductivity' with gap of the order of room temperature.

# The impact of disorder in 2D

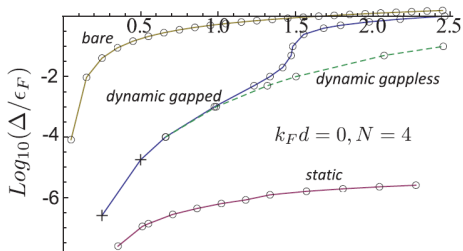
with Enrico Rossi, Rajdeep Sensarma, and Martin Rodriguez-Vega, and Sankar Das Sarma.

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Possibility 1: Excitonic gap is too small.

The form of the inter-layer screening used in the calculation of the gap is crucial:



Sodemann et al., Phys. Rev. B **85**, 195136 (2012).

For SiO<sub>2</sub> or BN substrates,  $\alpha = \frac{e^2}{\kappa \hbar v_F} \approx 0.5$ .  
For vacuum (suspended graphene),  $\alpha = 2.2$ .

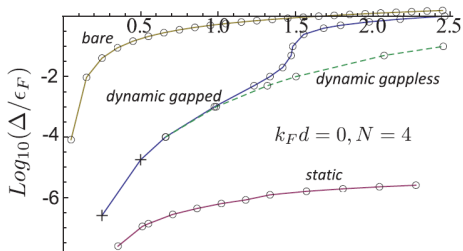
- **Unscreened interaction**  $\Rightarrow$  room temperature condensate!!!
- **Static screening**  $\Rightarrow$  vanishing gap.
- **Dynamic screening**  $\Rightarrow$  ???



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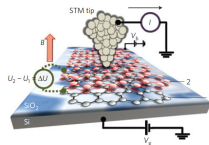
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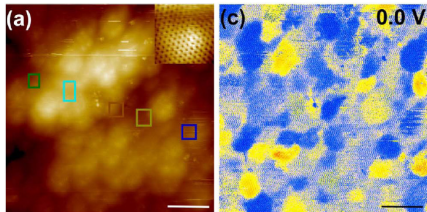
Possibility 2: Disorder

- STM can reveal atomic-scale structure of crystal.
- Also resolve the Dirac point,
- Which can be used to extract the local charge density.



Rutter *et al.*, Nat. Phys. **7**, 649 (2009).

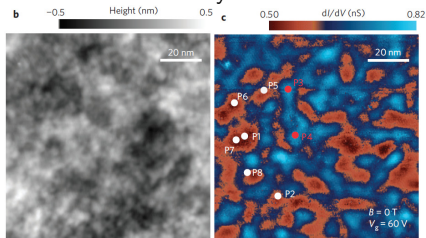
Monolayer:



Deshpande *et al.*, Phys. Rev. B **79**, 205411 (2009).

Scale bar is 8nm.

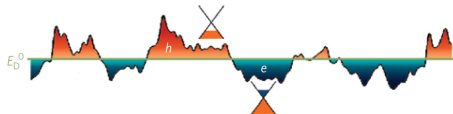
Bilayer:



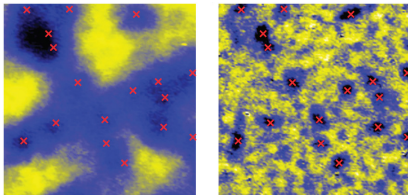
Rutter *et al.*, Nat. Phys. **7**, 649 (2011).

Scale bar is 20nm.

Scalar potential acts as a local shift in the chemical potential:

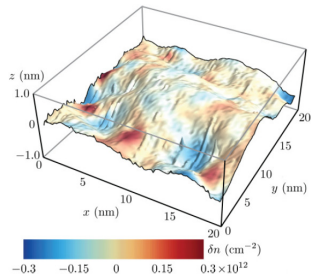


Charged impurities:



Zhang *et al.*, Nat. Phys. **5**, 722 (2009).

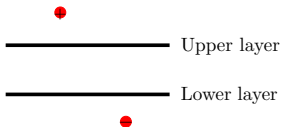
Ripples, corrugations, and strain:



Gibertini *et al.* Phys. Rev. B **85**, 201405(R) (2012).

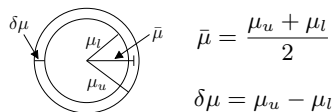
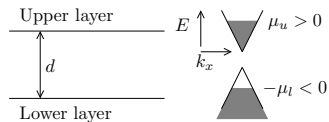
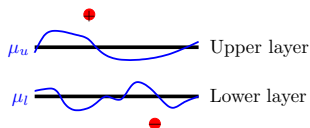


- Main question: Does charge inhomogeneity affect the formation of the condensate?





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- This is similar to magnetic disorder in superconductivity.

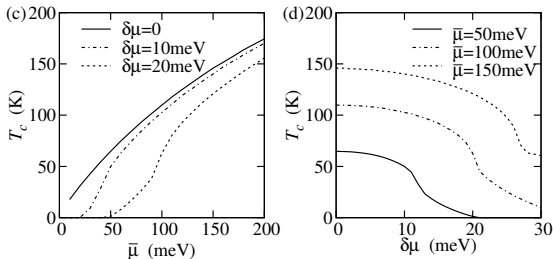
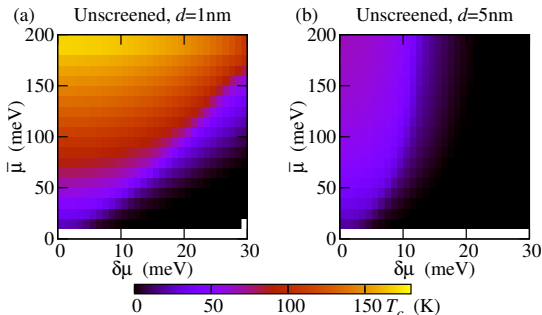
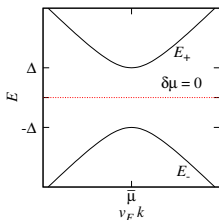
There are three stages to the calculation:

- ❶ Theory for **homogeneous unbalanced** system.
  - ▶ Temporarily ignore inhomogeneity, calculate effect of imperfectly nested Fermi surfaces.
- ❷ Analysis of realistic **inhomogeneity**.
  - ▶ Calculate statistics for  $\delta\mu(\mathbf{r})$  in situations corresponding to contemporary experiments.
- ❸ Combine these two results to assess impact of inhomogeneity on condensate formation.

Unscreened interaction:

$$V(q) = \frac{2\pi e^2}{\epsilon q}$$

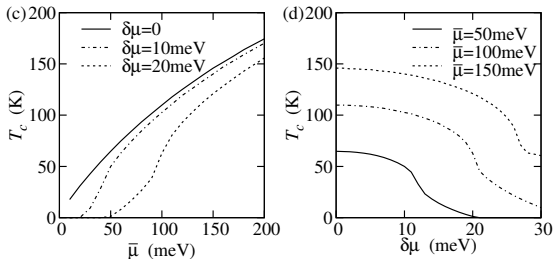
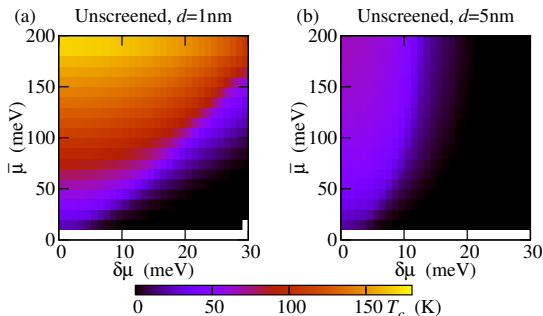
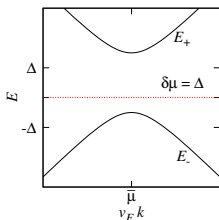
- $\Delta(\delta\mu)$  unchanged for  $\delta\mu < 2\Delta(0)$ .
- Equivalent to Clogston–Chandrasekhar limit.
- No evidence of FFLO state.



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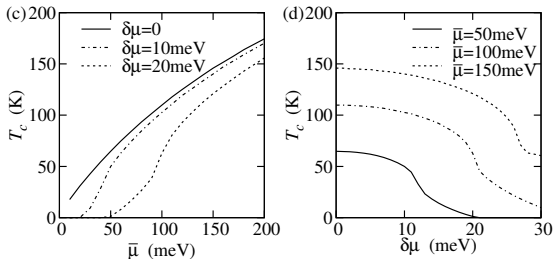
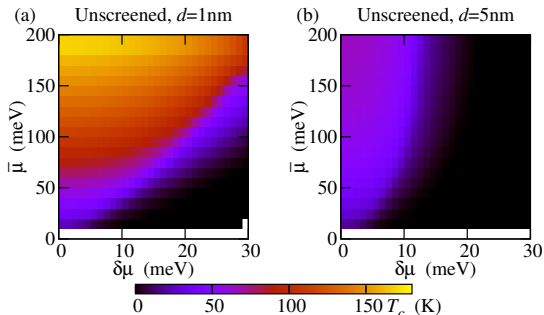
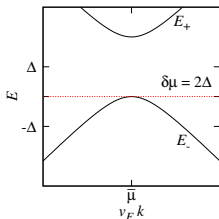




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- Broken translational symmetry makes it impossible to analytically calculate exact density distribution for random disorder.
- We employ a numerical method: [Thomas-Fermi theory](#).
- [Functional method](#) (à la DFT).
- The kinetic energy operator is also replaced by a functional of the density.
- This restricts the applicability to the regime where  $|\nabla n/n| < k_F$ , which is satisfied for double layer graphene.



- Energy functional is

$$E[n_u, n_l] = E_u[n_u(\mathbf{r})] + E_l[n_l(\mathbf{r})] + \frac{e^2}{2\kappa} \iint d^2\mathbf{r} d^2\mathbf{r}' \frac{n_u(\mathbf{r})n_l(\mathbf{r}')}{\sqrt{|\mathbf{r} - \mathbf{r}'|^2 + d^2}}$$

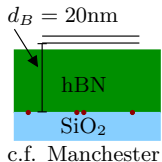
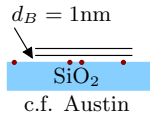
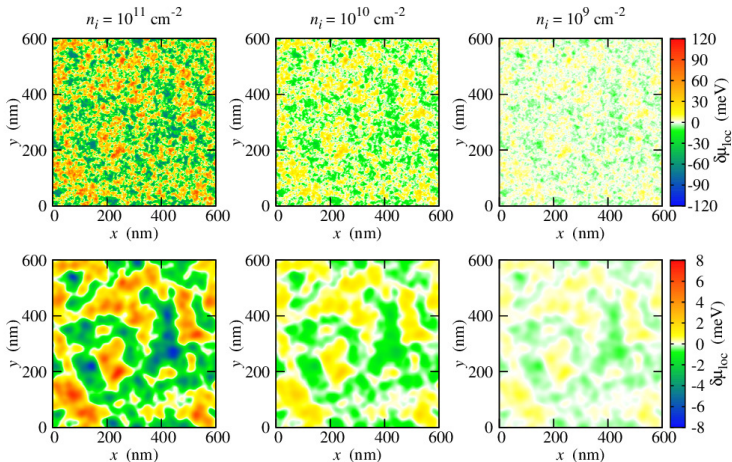
- Layer energy functional includes contributions from disorder potential, and electron–electron interactions:

$$E[n] = E_K[n(\mathbf{r})] + \frac{e^2}{2\kappa} \int d\mathbf{r}' \int d\mathbf{r} \frac{n(\mathbf{r})n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + \frac{e^2}{\kappa} \int d\mathbf{r} V_D(\mathbf{r})n(\mathbf{r}) - \mu \int d\mathbf{r} n(\mathbf{r}).$$

- Ground state density landscape is found by numerically minimizing the energy functional with respect to the density distribution.
- Density distribution gives local chemical potential for each layer, and hence the local  $\delta\mu$ .

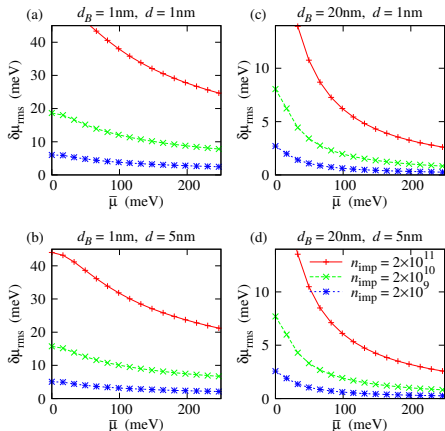


- Using TFT, we calculate the spatial profile of  $\delta\mu$  for a given manifestation of charged impurity disorder:





- We can perform this calculation for many ( $\approx 600$ ) disorder realizations and collect **statistics** for the distribution of  $\delta\mu$ .
- This distribution characterized by it's root-mean-square (rms) value.

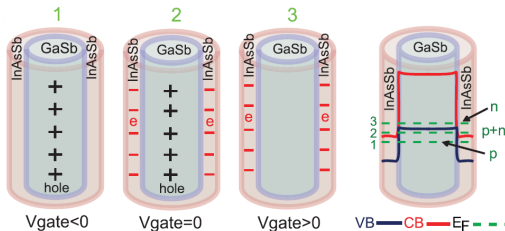
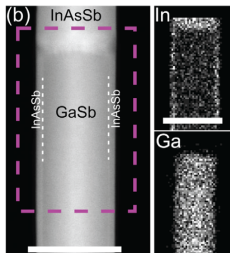


Predictions for  $\Delta$  from BCS theory:

- Unscreened:  $\Delta \sim 30\text{meV}$ ,
- Static screening:  $\Delta \sim 0.01\text{meV}$ ,
- Dynamic screening:  $\Delta \sim 1\text{meV}$ .

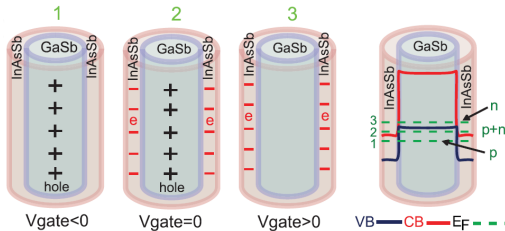
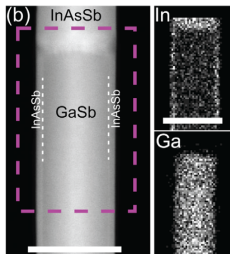
- Excitonic superfluidity is severely impacted by charge inhomogeneity in the two layers.
- The very cleanest contemporary samples may be on the cusp of allowing the condensate.
  - ▶ If estimates of the gap size using dynamical screening are to be believed.

## Generalization to 1D



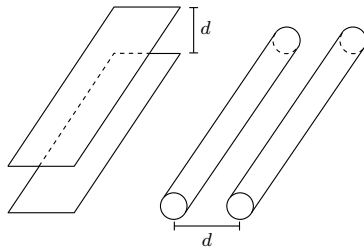
B. Ganjipour *et al.*, Appl. Phys. Lett. **101**, 103501 (2012).





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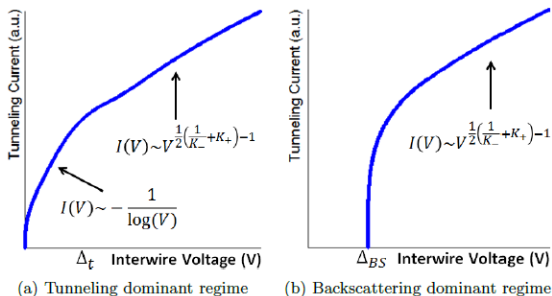
- Case 2 allows for pairing.
- Ground state populations.
- Alternate geometries also possible.



- No true long-range order in 1D.
- Particle correlations have power law decay  $\Rightarrow$  **quasi-order**.



- No true long-range order in 1D.
- Particle correlations have power law decay  $\Rightarrow$  **quasi-order**.
- In low density regime ( $k_F d < 1$ ), system is effectively fermionic.
- Transport experiments on core-shell wires show no Luttinger liquid behavior.  
B. Ganjipour *et al.*, Appl. Phys. Lett. **101**, 103501 (2012).
- Bosonization treatment by Werman and Berg:



Y. Werman and E. Berg, arXiv:1408.2718 (2014).

- Mean-field BCS theory in the particle-hole channel:

$$H = \sum_k \left[ \xi_{1k} a_k^\dagger a_k + \xi_{2k} b_{-k} b_{-k}^\dagger + \Delta_k a_k^\dagger b_{-k}^\dagger + \text{h.c.} \right].$$

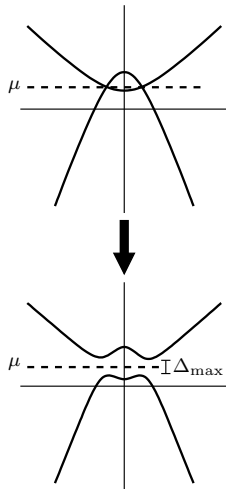
- The gap function is:

$$\Delta_k = \int dk' \frac{V_{\text{e-h}}(k' - k)}{4\pi} \frac{\Delta_{k'} [n_\alpha(k') + n_\beta(k') - 1]}{\sqrt{(\xi_{1k} - \xi_{2k})^2 + 4\Delta_{k'}^2}}.$$

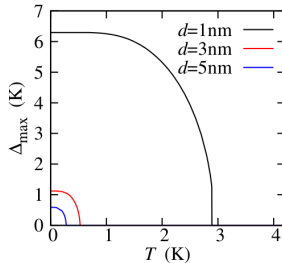
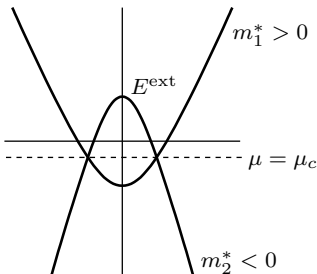
- Quasi-particle bands are:

$$E_{\pm k} = \frac{\xi_{1k} + \xi_{2k}}{2} \pm \frac{1}{2} \sqrt{(\xi_{1k} - \xi_{2k})^2 + 4\Delta_k^2}.$$

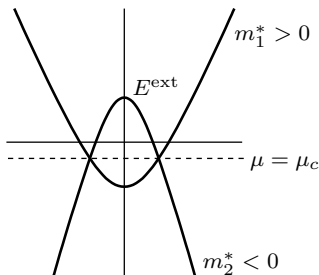
- Solve self-consistently for the gap function.
- Distance of closest approach of the two bands characterises 'condensate', label as  $\Delta_{\text{max}}$ .



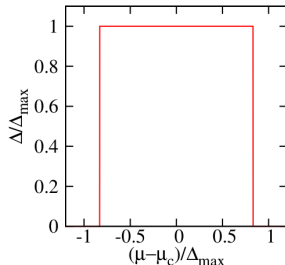
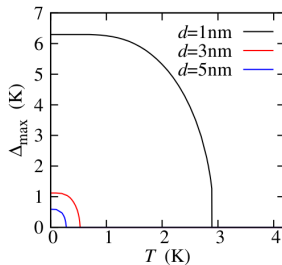
- Case 2 allows for pairing.
- Optimal pairing when  $\mu$  at band crossing ( $\mu_c$ ).



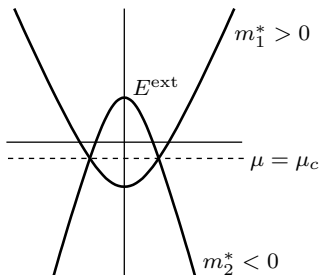
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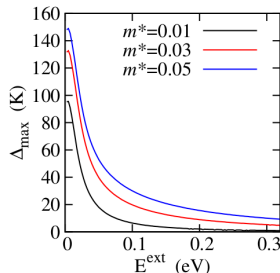
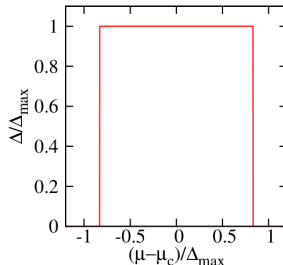
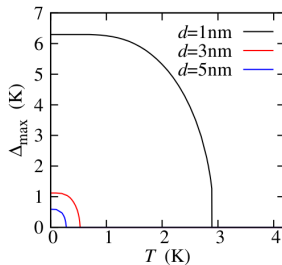
$$\mu_{\text{crit}} = \mu_c \pm 2\Delta_{\text{max}} \frac{\sqrt{|m_1^*||m_2^*|}}{|m_1^* - m_2^*|}$$



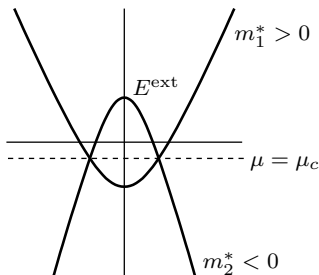
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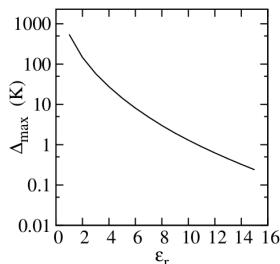
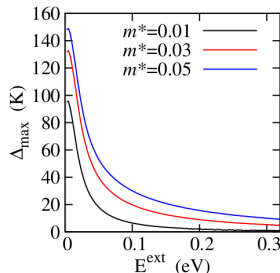
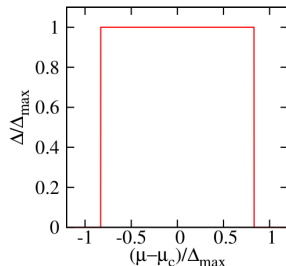
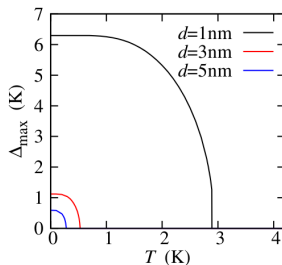
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- Spatially separated excitonic systems are an exciting avenue for device design.
- Double layer graphene systems may be on the cusp of realizing the condensate.  
[Phys. Rev. B \*\*86\*\*, 155447\(R\) \(2012\),](#)  
[Phys. Rev. B \*\*88\*\*, 235402 \(2013\).](#)

Collaboration with E. Rossi, S. Das Sarma, M. Rodriguez-Vega, and R. Sensarma.

- Parallel 1D systems may also be attractive hosts for exciton formation.  
[arXiv:1408.7065.](#)

- ‘Lateral heterostructures’ of 2D materials.
- Optical properties of 2D materials.
- Tunneling conductance in strongly correlated systems.

